Worksheet 01/17/2017

1. Find the following limits, provided they exist.

(a)
$$\lim_{x \to 0} \frac{3x - x^2}{x^2 - 4x + 3}$$

(b)
$$\lim_{x \to 3} \frac{3x - x^2}{x^2 - 4x + 3}$$

(c)
$$\lim_{x \to 1^{-}} \frac{3x - x^2}{x^2 - 4x + 3}$$

(d)
$$\lim_{x \to 1^+} \frac{3x - x^2}{x^2 - 4x + 3}$$

(e)
$$\lim_{x \to +\infty} \frac{3x - x^2}{x^2 - 4x + 3}$$

(f)
$$\lim_{x \to -\infty} \frac{3x - x^2}{x^2 - 4x + 3}$$

2. Find the following limits, provided they exist:

(a)
$$\lim_{x \to -1} \frac{\sqrt{x^2 + 8} - 3}{x + 1}$$

(b)
$$\lim_{x \to 2} \frac{8 - x^3}{x^3 - 5x + 2}$$

3. Find the following limits, provided they exist:

(a)
$$\lim_{x \to +\infty} \frac{2x}{\sqrt{9x^2 + 4}}$$

(b)
$$\lim_{x \to -\infty} \frac{2x}{\sqrt{9x^2 + 4}}$$

Does the function $f(x) = \frac{2x}{\sqrt{9x^2 + 4}}$ have horizontal asymptotes? If yes, describe them?

- **4.** Consider the function $f(x) = \frac{|x-5|}{x^2-25}$.
- (a) Does this function have horizontal asymptotes? Justify your answer with limits.
- (b) Does this function have vertical asymptotes? Justify your answer with limits.
- (c) Graph this function.