

1. Find the following limits, provided they exist.

$$(a) \lim_{x \rightarrow 3^+} \frac{2}{3-x}$$

$$(b) \lim_{x \rightarrow 3^-} \frac{2}{3-x}$$

$$(c) \lim_{x \rightarrow 3} \frac{2}{3-x}$$

$$(d) \lim_{x \rightarrow 0} \frac{3x-x^2}{x^2-4x+3}$$

$$(e) \lim_{x \rightarrow 3} \frac{3x-x^2}{x^2-4x+3}$$

$$(f) \lim_{x \rightarrow 1} \frac{3x-x^2}{x^2-4x+3}$$

$$(g) \lim_{x \rightarrow 2} \frac{x^2+x-6}{2-x}$$

$$(h) \lim_{x \rightarrow 2} \frac{x^2+x-6}{|2-x|}$$

2. Find the following limits, provided they exist:

$$(a) \lim_{x \rightarrow -1} \frac{\sqrt{x^2+8}-3}{x+1}$$

$$(b) \lim_{x \rightarrow 2} \frac{8-x^3}{x^3-5x+2}$$

3. Compute each of the following limits:

$$(a) \lim_{x \rightarrow 0} \frac{\sin(5x)}{x} =$$

$$\lim_{x \rightarrow 0} \frac{\sin(ax)}{x} =$$

$$(b) \lim_{x \rightarrow 0} \frac{\tan(3x)}{x} =$$

$$\lim_{x \rightarrow 0} \frac{\tan(bx)}{x} =$$

$$(c) \lim_{x \rightarrow 0} \frac{1 - \cos(x)}{x}$$

$$(d) \lim_{x \rightarrow 0} \frac{\tan^2(3x)}{x \sin(5x)}$$

$$(e) \lim_{x \rightarrow 0} \frac{\sin(3x^2) + x^2}{\sin^2(3x)}$$

$$(f) \lim_{x \rightarrow +\infty} x \tan(3/x) \text{ Hint: Use the substitution technique.}$$

$$(g) \lim_{x \rightarrow +\infty} \frac{\sin(5x)}{x} \text{ Hint: Be careful! Here } x \text{ does not go to zero!}$$