

Quiz 3

Name: \_\_\_\_\_

To receive credit you MUST SHOW ALL YOUR WORK.

1. Set up an integral (or integrals) that represent each of the following. You are NOT required to evaluate the integrals. A sketch the region or solid is required, along with the integral (or integrals).

(a) (5 pts) The area of region between the curves  $x = 2 - y^2$ ,  $x + y = 0 \Rightarrow x = -y$

$x = 2 - y^2$   
 $x + y = 0 \Rightarrow x = -y$   
 $y = \pm \sqrt{2 - x}$   
 $2 - y^2 = -y$   
 $y^2 + y - 2 = 0$   
 $(y - 2)(y + 1) = 0$   
 $y = 2, y = -1$

$\int_{-1}^2 (2 - y^2) - (-y) dy = \int_{-1}^2 (2 - y^2 + y) dy$

(b) (5 pts) The volume of the solid obtained when the region bounded by  $y = \sqrt{x}$ , the  $x$ -axis and the line  $x = 4$  is revolved around the line  $x = 4$ . Specify clearly what method you are using. You will receive 2 bonus points if you correctly solve the problem with both methods.

$y = \sqrt{x}$   
 $y^2 = x$   
 $\sqrt{x} = 4$   
 $x = 2$

**disk method**  
 $\int_0^2 \pi (4 - y^2)^2 dy$

**shell method**  
 $\int_0^4 2\pi (4 - x) \sqrt{x} dx$