

Name: \_\_\_\_\_

Panther ID: \_\_\_\_\_

Exam 2

Calculus II

Fall 2019

**Important Rules:**

1. Unless otherwise mentioned, to receive full credit you **MUST SHOW ALL YOUR WORK**. Answers which are not supported by work might receive no credit.
2. Please turn your cell phone off at the beginning of the exam and place it in your bag, **NOT** in your pocket.
3. Electronic devices (cell phones, calculators of any kind, etc.) should **NOT** be used at any time during the examination. Notes, texts or formula sheets should **NOT** be used either. Concentrate on your own exam. Do not look at your neighbor's paper or try to communicate with your neighbor.  
**Violations of any type of this rule will lead to a score of zero on this exam, possibly an automatic grade F for the course and a report for academic misconduct.**
4. Solutions should be concise and clearly written. Incomprehensible work is worthless.

1. (16 pts) Circle the correct answer (4 pts each):

(a) For the integral  $\int \sqrt{9x^2 - 1} dx$ , the following substitution is helpful:

- (i)  $3x = \sec \theta$       (ii)  $w = 9x^2 - 1$       (iii)  $w = \sqrt{9x^2 - 1}$       (iv)  $3x = \tan \theta$       (v)  $x = 3 \sin \theta$

(Don't spend time evaluating the integral. It is not required.)

(b) A parametrization for the ellipse  $\frac{x^2}{4} + \frac{y^2}{9} = 1$  is given by (assume  $0 \leq t \leq 2\pi$ )

- (i)  $x = \sin(2t)$ ,  $y = \cos(3t)$       (ii)  $x = 2t$ ,  $y = 3t$       (iii)  $x = 2 \sin(t)$ ,  $y = 3 \cos(t)$   
(iv)  $x = 2t$ ,  $y = 1 - 3t$       (v) none of the above

(c) Let  $T_4$  be the trapezoid approximation with 4 subdivisions of the integral  $\int_{-2}^2 (4 - x^2) dx$ . Then compared with the integral,  $T_4$  is an

- (i) overestimate      (ii) underestimate      (iii) exact estimate      (iv) cannot tell (more should be known)

(d) Let  $S_4$  be the Simpson approximation with 4 subdivisions of the integral  $\int_{-2}^2 (4 - x^2) dx$ . Then compared with the integral,  $S_4$  is an

- (i) overestimate      (ii) underestimate      (iii) exact estimate      (iv) cannot tell (more should be known)

**2.** (8 pts) Write an expression corresponding to  $M_4$ , the midpoint approximation with 4 subdivisions, for the integral  $\int_0^8 e^{-x^2} dx$ . Leave your answer in a calculator ready form, you DO NOT need to evaluate.

**3.** (8 pts) For the integral  $\int \frac{x+3}{(x+2)^2(x^2+1)} dx$

write the partial fraction decomposition and then find the integral, but DO NOT spend time to explicitly find the constants involved. It is NOT required.

**4.** (8 pts) The curve  $y = \ln x$ ,  $1 \leq x \leq e$  is rotated around the  $y$ -axis. Set up an integral that gives the surface area for the surface obtained. DO NOT spend time trying to evaluate the integral. It is NOT required.

For Problems 5-8, evaluate each integral.

5. (12 pts)  $\int \arcsin x \, dx$

6. (12 pts)  $\int_0^{\pi/4} \tan^2 x \sec^4 x \, dx$

7. (12 pts)  $\int \frac{1}{(9-x^2)^{3/2}} dx$

8. (12 pts)  $\int \frac{x-2}{x^2-4x+3} dx$

9. (10 pts) Evaluate the integral  $\int_0^{\pi/2} \cos^4 x \, dx$

You could use (without proof) the reduction formula below, or any other method.

$$\int \cos^n x \, dx = \frac{\cos^{n-1} x \sin x}{n} + \frac{n-1}{n} \int \cos^{n-2} x \, dx$$

**10.** Choose ONE. Note the different point values. If you do both, only the larger score will be considered for this problem, but the second score may give some bonus towards a previous problem where your score is smaller.

(A) (12 pts) Prove the reduction formula stated in Problem 9:

$$\int \cos^n x \, dx = \frac{\cos^{n-1} x \sin x}{n} + \frac{n-1}{n} \int \cos^{n-2} x \, dx$$

(B) (8 pts) State and prove the integration by parts formula.