

To receive credit you **MUST SHOW ALL YOUR WORK.**

1. (10 pts) (a) Assuming the pattern continues, find the next two terms of the sequence and give a formula for the general term a_n .

$$a_0 = 5, a_1 = 9, a_2 = 13, a_3 = 17, a_4 = 21, a_5 = \text{_____}, a_6 = \text{_____}, \dots, a_n = \text{_____}, \dots$$

(b) Assuming the pattern continues, find the next two terms of the sequence and give a formula for the general term a_n .

$$a_1 = \frac{1}{2}, a_2 = \frac{1}{6}, a_3 = \frac{1}{12}, a_4 = \frac{1}{20}, a_5 = \text{_____}, a_6 = \text{_____}, \dots, a_n = \text{_____}, \dots$$

2. (15 pts) (a) Let \mathcal{S}_n denote the set of all bit strings of length n . List all the elements in \mathcal{S}_3 . What is $|\mathcal{S}_3|$? What is $|\mathcal{S}_n|$?

(b) Let \mathcal{S}^f denote the set of all bit strings of finite length. Show that \mathcal{S}^f is infinitely countable. (Hint: What's the relation between \mathcal{S}^f and the \mathcal{S}_n 's?)

(c) Now let \mathcal{S} denote the set all bit strings of **infinite** length. Show that \mathcal{S} is not countable. (Hint: Use contradiction and Cantor diagonal argument.)