## MAP 2302 (Differential Equations)

TEST 2, Friday March 9, 2018
Name:
PID:
Remember that no documents or calculators are allowed during the test. You must show all your work to deserve the full credit assigned to any question. 3 pages.
1.[10] a) Show that the two functions $e^{x}$ and $x e^{-x}$ are linearly independent on the interval $(-\infty, 0]$.
b) Given that $0,0,0,3,1-2 \mathrm{i}, 1+2 \mathrm{i}, 1-2 \mathrm{i}, 1+2 \mathrm{i}, 1+\sqrt{2}, 1-\sqrt{2}, 9 \mathrm{i},-9 \mathrm{i}$ are the roots of the auxiliary equation corresponding to some 12 th-order homogeneous linear differential equation with constant coefficients, write down the general solution of the differential equation.
2. [10] Transform the Cauchy-Euler equation: $-3 x^{2} y^{\prime \prime}+7 x y^{\prime}-5 y=12 x^{3}, \quad x>0$, into a differential equation in the variable $t$ by setting $x=e^{t}$. You must show all the steps, but do not solve the differential equation in the variable $t$.
3. [20] Use the method of undetermined coefficients to solve the differential equation: $y^{\prime \prime}+9 y=3 x^{2}-4 x$.
4. [20] Use the variation of parameters method to solve the differential equation: $y^{\prime \prime}-2 y^{\prime}+y=\frac{e^{x}}{1+x^{2}}$

