Name:	Panther ID:				
Exam 1 - MAC2311 -	Spring 2016				
Important Rules:					
1. Unless otherwise mentioned, to receive not supported by work might receive no c 2. Please turn your cell phone off at the 3. No electronic devices (cell phones, cal nation. Notes, texts or formula sheets sh your neighbor's paper or try to community. Solutions should be concise and clearly	redit. beginning of the exam and place it in y lculators of any kind, etc.) should be u ould NOT be used either. Concentrate cate with your neighbor.	your bag, NOT in your pocket. used at any time during the examion your own exam. Do not look at			
1. (12 pts) These are True or False quest	tions. Circle your answer (2 pts) and b	oriefly justify (2 pts).			
(a) If $\lim_{x \to 3} f(x) = 6$ and $\lim_{x \to 3} g(x) = -1$	then $\lim_{x \to 3} (f(x) + 2g(x)) = 4$ Tr	rue False			
Justification:					
(b) The function $f(x) = \cot x$ is defined	and is continuous for all real numbers	x. True False			
Justification:					
(c) If $\lim_{x \to a} f(x) = 0$ and $\lim_{x \to a} g(x) = 0$ th	then $\lim_{x \to a} \frac{f(x)}{g(x)} = 0$ True Falson	se			
Justification:					
(d) The equation $x^3-8x+1=0$ has a re	eal solution in the interval [1,2].	True False			
Justification:					

2. (40 pts) Find the following limits (5 pts each). If the limit is infinite or does not exist, specify so.

(a)
$$\lim_{x \to 2} \frac{3x - 6}{x^2 - 5x + 6}$$

(b)
$$\lim_{x \to -3^-} \frac{1+2x}{x+3}$$

(c)
$$\lim_{t \to 2} \frac{|t-2|}{t^2-4}$$

(d)
$$\lim_{x \to -\infty} \frac{x - 4x^5}{1 + 2x^2 + 3x^4}$$

(e)
$$\lim_{x \to 0} \frac{\tan(5x)}{x + \sin(2x)}$$

(f)
$$\lim_{x \to -\infty} \frac{\sqrt{2x^2 + 1}}{x + 2}$$

(g)
$$\lim_{x \to 0} \frac{1 - \cos(3x)}{x^2}$$

(h)
$$\lim_{x \to +\infty} \frac{1 - \cos(3x)}{x^2}$$

- 3. (12 pts) Sketch the graph of ONE function f(x) satisfying ALL of the following conditions.
- (i) The function is defined and continuous everywhere except x=0 and x=3; The function is not defined at the points x=0 and x=3;

(ii)
$$\lim_{x\to 0} f(x) = -\infty$$
;

(iii)
$$\lim_{x\to 3^-} f(x) = -2$$
, $\lim_{x\to 3^+} f(x) = 0$;

(iv)
$$\lim_{x \to -\infty} f(x) = -2$$
, $\lim_{x \to +\infty} f(x) = 2$.

1	(10 ptc) II	o limite to	find the el	one of the	tangent li	no to the m	anh of f	$(x) - x^2 - $	3x at x = 3.
4.	TIO DOST OF		inna me si	оре от пте	tangent in	пе то гне вт	aph or 1	x - x - x	ou at $u - o$.

5. (10 pts) Given the function below

$$g(x) = \begin{cases} kx^2 - 1 & \text{if } x \le 1\\ 2x + k & \text{if } x > 1 \end{cases}$$

(a) (5 pts) Is there a value of the constant k which will make the function continuous? Justify your answer.

(b) (5 pts) Sketch the graph of the function g(x) when k=1. Label carefully the coordinates of important points.

6. (a) (3 pts) Write the general (ϵ, δ) definition for $\lim_{x \to a} f(x) = L$.

Choose ONE of the parts (b) and (c). Only ONE will receive credit. Note the different point values.

- (b) (7 pts) Use the (ϵ, δ) definition to prove $\lim_{x \to -2} (5x+4) = -6$.
- (c) (12 pts) Use the (ϵ, δ) definition to prove $\lim_{x\to 2} (2x^2+3) = 11$.

- 7. (10 pts) Choose ONE of the following:
- (a) State and prove the quadratic formula.
- (b) Using the inequality $\sin x \le x \le \tan x$ for any $x \in (0, \pi/2)$, show that $\lim_{x \to 0^+} \frac{\sin x}{x} = 1$.