1. Suppose $\mathcal{C}$ is a circle and that $L_{1}$ is a secant line that intersects the circle at $A$ and $B$. Let $L_{2}$ be the tangent line to the circle at $A$. Show that the angles between $L_{1}$ and $L_{2}$ at $A$ are each equal to $1 / 2$ of the measure of the corresponding arc determined by the chord $A B$ on the circle (there are two such arcs whose sum of measures is $360^{\circ}$ ).
2. Suppose $\mathcal{C}$ is a circle, that $L_{1}$ and $L_{2}$ are two lines secants to the circle and assume that $L_{1} \cap L_{2}=\{P\}$ where $P$ is a point in the interior of the circle. Find and prove formulae for the angles at $P$ between $L_{1}$ and $L_{2}$ in terms of the arcs determined on the circle by the 4 points of intersection with the two secants.
3. Suppose $\mathcal{C}$ is a circle and assume that $A$ and $B$ are points on the circle. Denote by $L_{1}$ and $L_{2}$ the tangent lines to the circle at $A$, respectively $B$. Find and prove a formula for the (acute) angle between $L_{1}$ and $L_{2}$ in terms of the arcs determined by the points $A$ and $B$ on the circle.
