## **Suggested Problems** — on the general topic of cyclic quadrilaterals MTG 3212 2010

**1.** Show that a quadrilateral is cyclic if and only if one side subtends equal angles at the other two vertices.

**2.** Suppose  $\triangle ABC$  is an acute triangle and let D, E, F denote the feet of altitudes from A, B, C, respectively.

Show that the orthocenter H of the triangle  $\triangle ABC$  is the incenter of the triangle  $\triangle DEF$ .

Note: The triangle  $\triangle DEF$  is called the *orthic* triangle of the triangle  $\triangle ABC$ .

**3.** Show that a quadrilateral is a tangent quadrilateral if and only if the sums of the pairs of opposite sides are equal.

Note: This is Theorem 39 in your textbook. I am asking you to figure out, or understand the proof on your own.