

MAC2312 Section U03

Suggested problems for final exam.

The final exam is **cumulative**.

You should **also** practice the suggested problems for Tests 1 through 3.

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1. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{1}{5k+2}$$

2. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{1}{k(k+1)}$$

3. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{k}{1+k^2}$$

4. Determine whether the series converges or diverges.

$$\sum_{k=2}^{\infty} \frac{\ln k}{k}$$

5. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{1}{\sqrt{k^2 + 1}}$$

6. Determine whether the series converges or diverges.

$$\sum_{k=2}^{\infty} \frac{1}{\ln k}$$

7. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{1}{3^k + 5}$$

8. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{1}{(2k+3)^{17}}$$

9. Determine whether the series converges or diverges.

$$\sum_{k=0}^{\infty} \frac{1}{k!}$$

10. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{k^2}{5^k}$$

11. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{1}{1 + \sqrt{k}}$$

12. Determine whether the series converges or diverges.

$$\sum_{k=2}^{\infty} \frac{\ln k}{2^k}$$

13. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{(-1)^{k+1}}{3k}$$

14. Determine whether the series converges or diverges.

$$\sum_{k=1}^{\infty} \frac{\cos(k\pi)}{k}$$

**15.** Determine whether the series converges absolutely, converges conditionally, or diverges.

$$\sum_{k=1}^{\infty} \frac{(-1)^k}{k}$$

**16.** Determine whether the series converges absolutely, converges conditionally, or diverges.

$$\sum_{k=1}^{\infty} \frac{(-1)^k}{k^{4/3}}$$

**17.** Determine whether the series converges absolutely, converges conditionally, or diverges.

$$\sum_{k=0}^{\infty} \frac{(-1)^k}{k!}$$

**18.** Determine whether the series converges absolutely, converges conditionally, or diverges.

$$\sum_{k=2}^{\infty} \frac{(-1)^k \ln k}{k}$$

**19.** Determine whether the series converges absolutely, converges conditionally, or diverges.

$$\sum_{k=0}^{\infty} \left(\frac{-3}{5}\right)^k$$

20. Find the Maclaurin series for the function.

$$f(x) = e^{-x}$$

**21.** Find the Maclaurin series for the function.

$$f(x) = e^{5x}$$

**22.** Find the Maclaurin series for the function.

$$f(x) = \frac{1}{1+x}$$

**23.** Find the Maclaurin series for the function.

$$f(x) = \ln(1 + x)$$

24. Find the Maclaurin series for the function.

$$f(x) = (1 + x)^{1/4}.$$

**25.** Find the Maclaurin series for the function.

$$f(x) = (1 + 2x)^{1/3}.$$

**26.** Find the Maclaurin series for the function.

$$f(x) = xe^x$$

**27.** Find the Maclaurin series for the function.

$$f(x) = x \sin x$$

**28.** Find the Maclaurin polynomial of degree 2 for  $f(x) = \cos x$ , and use it to estimate  $\cos(0.1)$  to the nearest thousandth.

**29.** Find the Maclaurin polynomial of degree 3 for  $f(x) = \ln(1 + x)$ , and use it to estimate  $\ln(1.1)$  to the nearest ten thousandth.