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MAC 2313 Quiz 2  
Thursday January 18th

Find the angle between the vectors  $\mathbf{u} = \langle 2, 1, 1 \rangle$  and  $\mathbf{v} = \langle 1, 0, 1 \rangle$ .

We know  $\vec{u} \cdot \vec{v} = |\vec{u}| |\vec{v}| \cos \theta$

where  $\theta$  is the angle between  $\vec{u}$  and  $\vec{v}$ .

$$\text{Hence } \cos \theta = \frac{\vec{u} \cdot \vec{v}}{|\vec{u}| |\vec{v}|} = \frac{2 \cdot 1 + 1 \cdot 0 + 1 \cdot 1}{\sqrt{2^2 + 1^2 + 1^2} \cdot \sqrt{1^2 + 0^2 + 1^2}}$$

$$= \frac{3}{\sqrt{6} \sqrt{2}} = \frac{3}{\sqrt{12}} = \frac{3}{\sqrt{4} \sqrt{3}} = \frac{\sqrt{3}}{2}$$

$$\text{So } \theta = \arccos \frac{\sqrt{3}}{2} = \frac{\pi}{6} \text{ or } 30^\circ$$