Exam #1, ver B

January 30, 2017

Name ______

- You will be told when to begin the work and when to terminate work on the examination. You must stop when instructed. Points may be deducted in case of violations.
- Please show your work to support your answers that require calculations. Correct but unsupported answers may not be given full credit.
- The use of a cell phone or other electronic communication devices during the examination is not allowed. The exam will be canceled and a grade of "0" will be assigned to anyone who uses a cell phone during the examination or if one is found within hands reach.
- Calculators are not allowed on this exam.
- The exam consist of two parts. Part I contains five multiple choice questions worth 5 points each. Part II contains 7 open ended questions worth 12 points each if not stated otherwise.

Part I

Choose your answer from five available choices. No partial credit will be given for wrong answers.

1. If $f(x) = \frac{4}{x}$ and $g(x) = \frac{2}{x+3}$, then $(f \circ g)(x)$ is (a) 2x + 6(b) $\frac{2}{3x+4}$ (c) $\frac{2x}{3x+4}$

$$3x + 2x$$

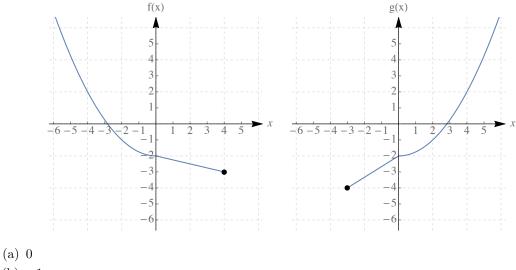
(d)
$$\frac{1}{x+3}$$

(e) None of the above

The domain of $f \circ g$ is

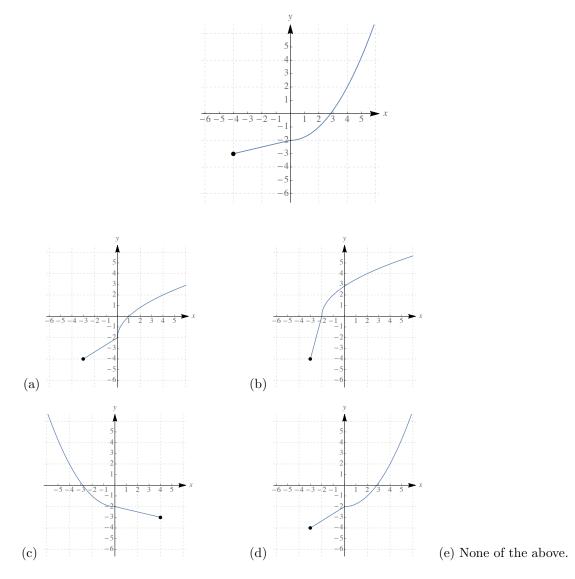
- (a) $(0,\infty)$
- (b) $(-\infty,\infty)$
- (c) $(-\infty, -3) \cup (-3, \infty)$
- (d) $(-\infty, -4/3) \cup (-4/3, 0) \cup (0, \infty)$
- (e) None of the above.

2. The graphs of f(x) and g(x) are given below. The value of (f+g)(-3) is



- (b) −1
- (c) -3
- (d) -4
- (e) None of the above.
- 3. If f is one-to-one and f(-2) = 7, then which of the following statements are true? (Select all true statements.)
 - (a) f is even
 - (b) $f^{-1}(7) = 2$
 - (c) (1,7) is on the graph of y = f(-2x)
 - (d) (-2,7) is on the graph of the graph of f
 - (e) None of the above.

4. The graph of a one-to-one function f is given below. Which of the following is the graph of its inverse?

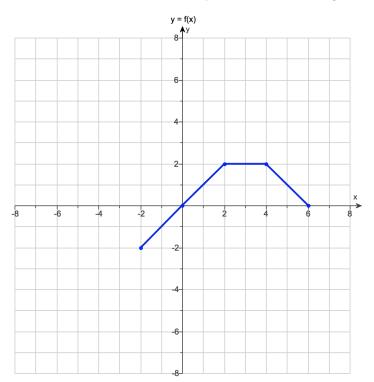


- 5. If the graph of the function $y = x^2$ is vertically stretched by a factor of 2 and then shifted to the left by 5 then the resulting function has the equation
 - (a) $y = 2x^2 + 5$
 - (b) $y = 2x^2 5$
 - (c) $y = 2(x-5)^2$
 - (d) $y = 2(x+5)^2$
 - (e) None of the above.

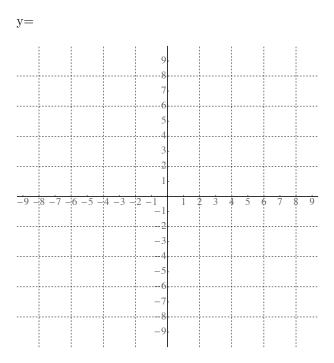
Part II

6. Graph the function $f(x) = \begin{cases} \sqrt{-x} & , x < -1 \\ x^2 & , -1 \le x \le 2 \\ x - 2 & x > 2 \end{cases}$									
				9					
				8					
				7	-				
				6 5					
				3	-				
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-9 -	8 -7 -	6 - 5 -	4 -3 -	2 - 1 - 1	1 2	2 3 4	1 5 (57	8 9
				2					
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				-9					
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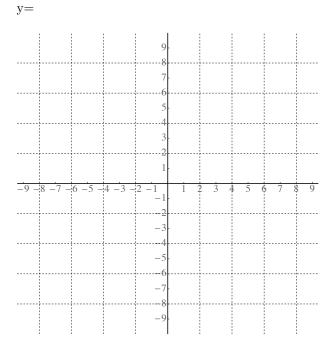
7. Given the graph of f(x), use transformations to graph y = -2f(-x+3). Do one transformation at a time. Name the transformation and write the equation of the resulting function.



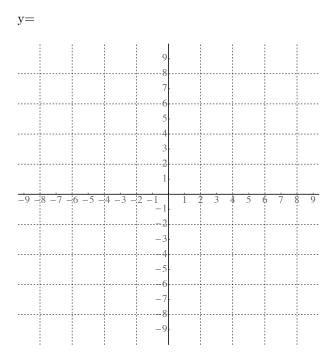
(i) transformation:



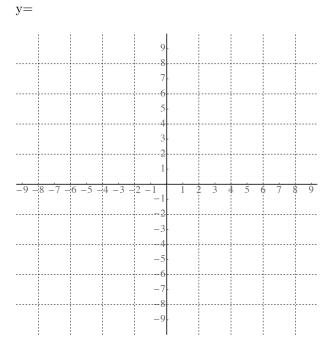
(ii) transformation:



(iii) transformation:



(iv) transformation:

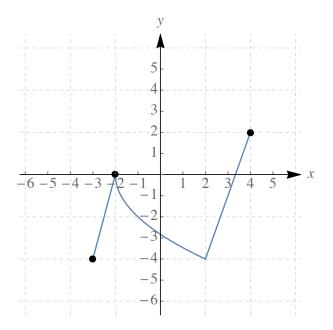


8. Find the difference quotient for $f(x) = \frac{2}{x-3}$.

9. Find the inverse of $f(x) = \frac{3}{x} + 2$

10. Find the domain of $f(x) = -3\sqrt{2x+5}$

11. Using the given graph of the function f, answer the parts (a)-(f) below.



- (a) Find the domain of f. Express it in interval notation.
- (b) Find the range of f. Express it in interval notation.
- (c) Find the x-intercepts.
- (d) Find the y-intercepts.
- (e) Find the intervals on which f is increasing.
- (f) Find the intervals on which f is decreasing.

12. (13 points) Find two functions f(x) and g(x) (neither of them identity) so that h(x) = f(g(x)), where
7

$$h(x) = \frac{7}{(3x-7)^3}$$