

MAC2233 - Review for exam 4

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Find the indicated integral. Check your answers by differentiation.

$$1) \int \sqrt{t} dt$$

1) _____

$$2) \int 8e^x dx$$

2) _____

$$3) \int (x^{1/3} - 4x^{-2/3} + 4) dx$$

3) _____

$$4) \int \left(9e^u + \frac{9}{u} + \ln 5 \right) du$$

4) _____

$$5) \int e^{-0.01t}(e^{-0.14t} + 7) dt$$

5) _____

Solve the given initial value problem for $y = f(x)$.

$$6) \frac{dy}{dx} = 3x - 5 \text{ where } y = 3 \text{ when } x = -1$$

6) _____

$$7) \frac{dy}{dx} = \frac{6}{x} - \frac{1}{x^2} \text{ where } y = -5 \text{ when } x = 1$$

7) _____

The slope $f'(x)$ at each point (x, y) on a curve $y = f(x)$ is given along with a particular point (a, b) on the curve. Use this information to find $f(x)$.

$$8) f'(x) = 9x^2 - 8x + 2; (0, 7)$$

8) _____

$$9) f'(x) = e^{-x} + x^7; (0, -9)$$

9) _____

Solve the problem.

- 10) A manufacturer estimates that the marginal cost of producing q units of a certain commodity is $C'(q) = 3q^2 - 12q + 12$ dollars per unit. If the cost of producing 10 units is \$2000, what is the cost of producing 20 units?

- 11) Suppose the consumption function for a particular country is $c(x)$, where x is national disposable income. Then the marginal propensity to consume is $c'(x)$. Suppose x and c are both measured in billions of dollars and

$$c'(x) = 0.8 + 0.3\sqrt{x}$$

If consumption is 14 billion dollars when $x = 0$, find $c(x)$.

Find the indicated integral.

12) $\int e^{3x-5} dx$

12) _____

13) $\int \sqrt{8x+4} dx$

13) _____

14) $\int 2xe^{x^2+2} dx$

14) _____

15) $\int \frac{1}{x \ln x} dx$

15) _____

Evaluate the given definite integral using the fundamental theorem of calculus.

16) $\int_{-3}^3 (8x - 3) dx$

16) _____

17) $\int_1^4 2\sqrt{u} du$

17) _____

18) $\int_5^7 (8 + 2t + 3t^2) dt$

18) _____

19) $\int_2^3 (2x - 5)^4 dx$

19) _____

$$20) \int_{1/6}^{1/4} \frac{e^{1/x}}{x^2} dx$$

20) _____

Solve the problem.

- 21) A study indicates that t months from now the population of a certain town will be growing at the rate of $P'(t) = 6 + 5t^{2/3}$ people per month. By how much will the population of the town increase over the next 6 months?

21) _____

Answer Key

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$$1) \frac{2t^{3/2}}{3} + C$$

$$2) 8e^x + C$$

$$3) \frac{3x^{4/3}}{4} - 12x^{1/3} + 4x + C$$

$$4) 9e^u + 9 \ln|u| + (\ln 5)u + C$$

$$5) -\frac{20}{3}e^{-0.15t} - 700e^{-0.01t} + C$$

$$6) y = \frac{3}{2}x^2 - 5x - \frac{7}{2}$$

$$7) y = \ln x^6 + \frac{1}{x} - 6$$

$$8) f(x) = 3x^3 - 4x^2 + 2x + 7$$

$$9) f(x) = -e^{-x} + \frac{x^8}{8} - 8$$

10) \$7320

$$11) c(x) = 0.8x + 0.2x^{3/2} + 14$$

$$12) \frac{1}{3}e^{3x-5} + C$$

$$13) \frac{1}{12}(8x+4)^{3/2} + C$$

$$14) ex^2 + 2 + C$$

$$15) \ln|\ln x| + C$$

16) -18

$$17) \frac{28}{3}$$

18) 258

19) 0.2

$$20) e^6 - e^4$$

21) About 95 people