

In each case, c represents a positive real number.

To Graph:	Draw the Graph of f and:	Changes in the Equation of $y = f(x)$
Vertical shifts $y = f(x) + c$ $y = f(x) - c$	Raise the graph of f by c units. Lower the graph of f by c units.	c is added to $f(x)$. c is subtracted from $f(x)$.
Horizontal shifts $y = f(x + c)$ $y = f(x - c)$	Shift the graph of f to the left c units. Shift the graph of f to the right c units.	x is replaced with $x + c$. x is replaced with $x - c$.
Reflection about the x -axis $y = -f(x)$	Reflect the graph of f about the x -axis.	$f(x)$ is multiplied by -1 .
Reflection about the y -axis $y = f(-x)$	Reflect the graph of f about the y -axis.	x is replaced with $-x$.
Vertical stretching or shrinking $y = cf(x), c > 1$ $y = cf(x), 0 < c < 1$	Multiply each y -coordinate of $y = f(x)$ by c , vertically stretching the graph of f . Multiply each y -coordinate of $y = f(x)$ by c , vertically shrinking the graph of f .	$f(x)$ is multiplied by $c, c > 1$. $f(x)$ is multiplied by $c, 0 < c < 1$.
Horizontal stretching or shrinking $y = f(cx), c > 1$ $y = f(cx), 0 < c < 1$	Divide each x -coordinate of $y = f(x)$ by c , horizontally shrinking the graph of f . Divide each x -coordinate of $y = f(x)$ by c , horizontally stretching the graph of f .	x is replaced with $cx, c > 1$. x is replaced with $cx, 0 < c < 1$.

1. A project requires the transformation of the cubic function to the function $h(x) = -(x - 2)^3 + 4$. You are supervising Wells and Anderson and they have a dispute over the proper order of the transformation that you will have to write into a computer program.

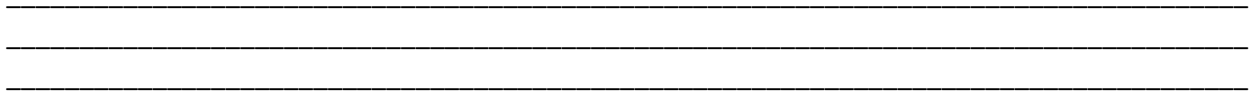
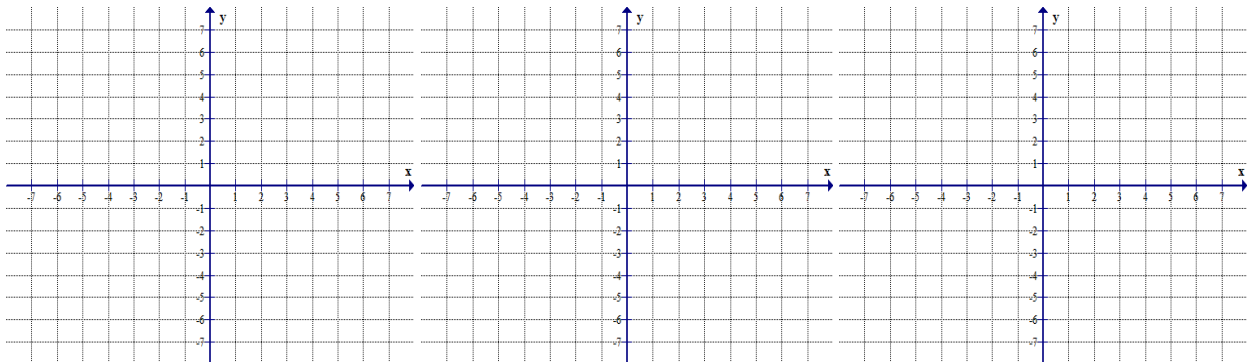
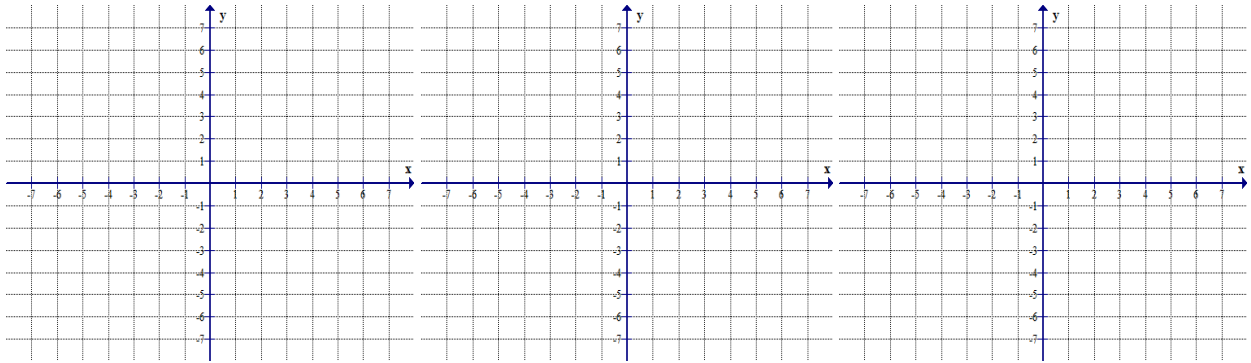
Wells says that the transformation should be:

- i. Shift right 2
- ii. Shift up 4
- iii. Reflect across the x axis

Anderson says:

- i. Shift right 2
- ii. Reflect across the x axis
- iii. Shift up 4

They are bickering. You need to settle this and use it as a teaching moment so they both know the correct transformation (and why it is correct) for future projects. Graph both set of transformations and determine which set results in the graph $h(x) = -(x - 2)^3 + 4$. Explain who is correct and why.



2. Suppose Point A is $(1,3)$ and is a point on the graph of $y = g(x)$. You are asked to transform the graph of $g(x)$ so that y is now equal to $g(x+3) - 5$. Where is Point A now located? Use the graphs below to show each how each transformation changes the starting point, A.

