MAC 1140, Fall 2017

Exam #5

December 4, 2017

Name			

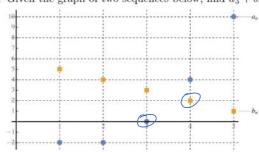
- You will be told when to begin the work and when to terminate work on the examination. You must stop when instructed. Points may be deducted in case of violations.
- Please show your work to support your answers that require calculations. Correct but unsupported answers may not be given full credit.
- The use of a cell phone or other electronic communication devices during the examination is not allowed. The exam will be canceled and a grade of "0" will be assigned to anyone who uses a cell phone during the examination or if one is found within hands reach.
- Calculators are not allowed on this exam.
- The exam consist of two parts. Part I contains five multiple choice questions worth 5 points each. Part II contains 6 open ended questions.

Part I

Choose your answer from five available choices. No partial credit will be given for wrong answers.

- 1. Find the term containing x^9 in the expansion of $(x+3)^{12}$
 - (a) $\binom{12}{3} x^9 3^9$
 - (b) $\binom{12}{9}x^93^3$ (c) $\binom{12}{3}x^93^3$
- Since $\binom{12}{9} = \binom{12}{3}$
- (d) $\binom{9}{12}x^93^3$
- (e) None of the above
- 2. Compute the binomial coefficient (6)
- $\frac{6!}{3!3!} = \frac{\cancel{6.5 \cdot 4.3!}}{\cancel{3 \cdot 3 \cdot 3 \cdot 2 \cdot 1}} = 20$

- (a) 15
- (b) 20
- (c) 30
- (d) 40
- (e) None of the above
- 3. Given the graph of two sequences below, find $a_3 + b_4$.



0+2=2

- (a) 0
- (b) 1
- (c) 2
- (d) 3
- (e) None of the above
- 4. Evaluate $\sum_{k=1}^{5} k(k-1) = 1.0 + 2.1 + 3.2 + 4.3 + 5.4 = 2 + 6 + 12 + 2.0$ = 40
 - (a) 30
 - (b) 35
 - (c) 40
 - (d) 50
 - (e) None of the above
- 5. The sequence $\frac{1}{2}$, 3, 18, 108, . . . is

 - (a) arithmetic
 - (b) geometric
 - (c) neither

$$\frac{3}{2} = \frac{3 \cdot 2}{18} = \frac{108}{18} = \frac{6}{18}$$

$$\frac{18}{3} = 6$$

Part II

6. (a) (10 pts) Find the general formula for 1, 4, 7, 10, 13, ...

$$\alpha_n = (+3(n-1))$$

(b) (6 pts) Find a_{100} .

(c) (10 pts) Find the sum $1 + 4 + 7 + 10 + 13 + \cdots + 121$.

$$S_{41} = \frac{41}{2} \cdot (1 + (21))$$

$$= \frac{41}{2} \cdot \frac{122}{1} = \boxed{41.61}$$

$$= \boxed{2501}$$

|2| = |+ 3(n-1) $\frac{|20|}{3} = \frac{3(n-1)}{3}$ 40 = n-1

7. (a) (10 pts) Given $a_3 = 4$ and $r = \frac{1}{2}$, find the 7th term of this sequence.

$$a_4 = 4 \cdot \frac{1}{2} = 2$$
 $a_5 = 2 \cdot \frac{1}{2} = 1$
 $a_6 = 1 \cdot \frac{1}{2} = \frac{1}{2}$

az = 2 = 4

(b) (8 pts) Write the sum of the first 20 terms or this sequence. Do not evaluate or simplify.

$$\alpha_3 = 4 = \alpha_1 r^{34}$$

$$4 = \alpha_1 \cdot \left(\frac{1}{2}\right)^2$$

$$4 = \alpha_1 \cdot 4$$

$$S_{20} = \frac{16(1-(\frac{1}{2})^{20})}{1-\frac{1}{2}}$$

8. (12 pts) Write the sum in sigma notation
$$\frac{1}{2} + \frac{2}{4} + \frac{3}{8} + \frac{4}{16} + \frac{5}{32} + \dots + \frac{10}{1024}$$
.

9. (12 pts) Expand
$$(1-2x)^5$$
 using the Binomial theorem. Any other method will result in zero pts.

$$= {5 \choose 0} {1 \choose (-2x)} + {5 \choose 1} {1 \choose (-2x)} + {5 \choose 2} {1 \choose 2} {1 \choose 2} {1 \choose 2} {1 \choose 3} {1 \choose 4} {1 \choose 5} {1 \choose 5} {1 \choose 2} {1 \choose 5} {1 \choose 2} {1 \choose 2} {1 \choose 3} {1 \choose 2} {1 \choose 3} {1 \choose 4} {1 \choose 5} {1 \choose 5$$

10. (7 pts) Find the 5th term of the sequence given by the recursive formula:
$$a_1 = 1, a_n = n \cdot a_{n-1}$$
.

$$\alpha_2 = 2 \cdot 1 = 2$$
 $\alpha_3 = 2 \cdot 3 = 6$
 $\alpha_4 = 6 \cdot 4 = 24$
 $\alpha_5 = 24 \cdot 5 = 120$

11. Evaluate the expression

(a)
$$(5 \text{ pts}) \frac{5!}{3!} = \frac{5 \cdot (\cdot, 3)}{3!} = \frac{20}{3!}$$

(b)
$$(5 \text{ pts}) \frac{(n+2)!}{n!} = \frac{(n+2)(n+1)}{m!} = \frac{(n+2)(n+1)}{m!} = \frac{n^2}{3n+2}$$