

Exam 1 on Monday, 9/25

↳ Chapter 2 & section 3.2

Exam 1 review on Saturday, 9/23, 10am-noon in

MMC CP 145.

A professor will mostly answer student's questions

Online review available on mathstat.fiu.edu. Look for the link on the second page in syllabus.

Section 2.7

Note: A function, $f(x)$, is **one-to-one** if it has an inverse.

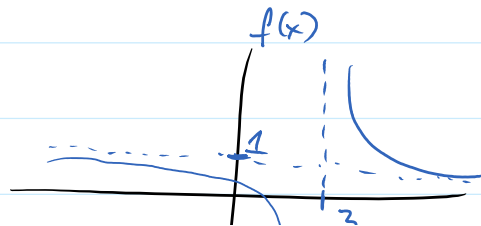
Ex: find f^{-1} , if $f(x) = \frac{x+2}{x-3}$, $x \neq 3$.

$$y = \frac{x+2}{x-3} \Leftrightarrow x = \frac{y+2}{y-3}$$

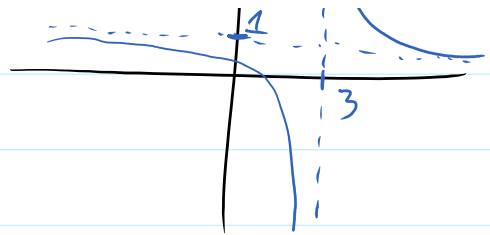
$$x(y-3) = y+2$$

$$xy - 3x = y + 2$$

	f	f^{-1}
domain	$(-\infty, 3) \cup (3, \infty)$	$(-\infty, 1) \cup (1, \infty)$
range	$(-\infty, 1) \cup (1, \infty)$	$(-\infty, 3) \cup (3, \infty)$



$$\begin{aligned}
 xy - 3x &= y + 2 \\
 xy - y &= 3x + 2 \\
 y(x-1) &= 3x + 2
 \end{aligned}$$



$$y = \frac{3x+2}{x-1}$$

$$f^{-1}(x) = \frac{3x+2}{x-1}$$

Domain: $(-\infty, 1) \cup (1, \infty)$

f is one-to-one.

Section 3.2 - Polynomials

	degree	leading coef.
$x-3$ ✓	1	1
x^4+x-2 ✓	4	1
x^2+x^{-2} X	X	X
$-3x^4 - \frac{1}{x} = -3x^4 - x^{-1}$ X	X	X
$-x^2 + x^0 = -x^2 + 1$ ✓	2	-1

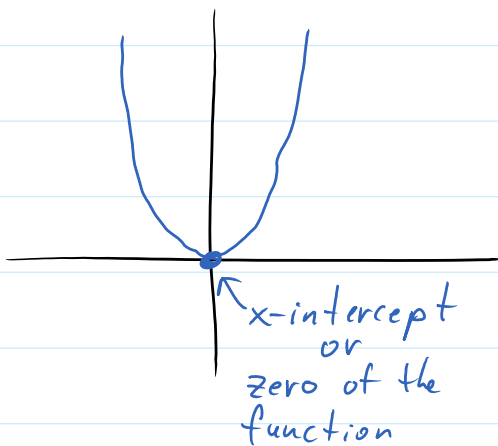
Def: let n be a nonnegative integer and let $a_n, a_{n-1}, \dots, a_1, a_0$ be real numbers, with $a_n \neq 0$. The function defined by

$$a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

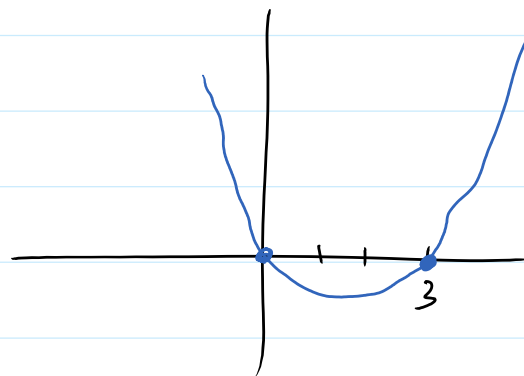
is called a polynomial function of degree n . The number a_n is called the **leading coefficient**.

Graphing a polynomial function

$$f(x) = x^2$$

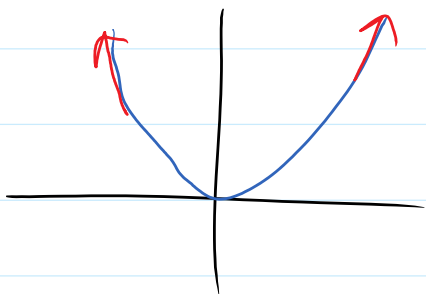


$$f(x) = x^2 - 3x = x(x-3)$$

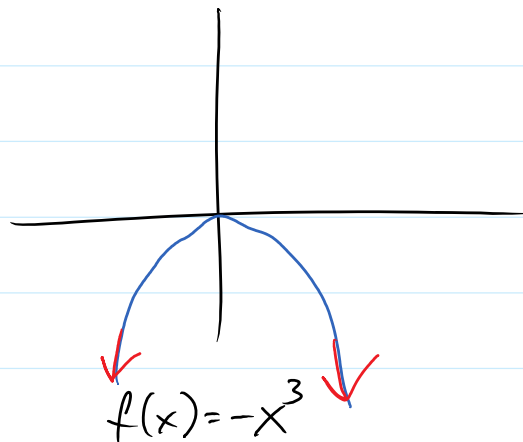


$$f(x) = x^3 + 2x^2 - x + 3$$
$$f(x) = x(x-3)^4(x-1)^2$$

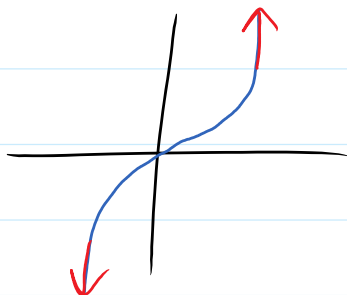
$$f(x) = x^2$$



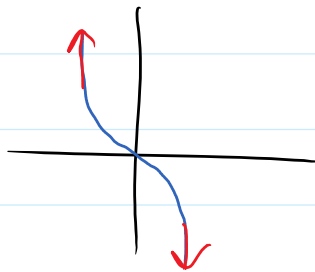
$$f(x) = -x^2$$



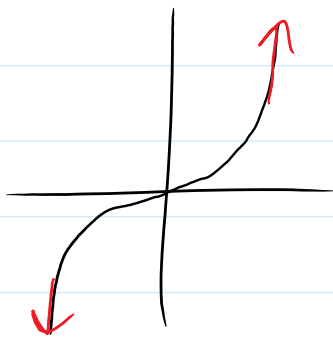
$$f(x) = x^3$$



$$f(x) = -x^3$$



$$f(x) = x^7 \Leftrightarrow \text{looks like } x^3$$



Leading coefficient test

As x increases or decreases without bound, the graph of the polynomial will have the following end behavior:

		degree	
		odd	even
Sign of the leading coefficient	+	↙ ↘	↖ ↗
	-	↗ ↘	↙ ↘

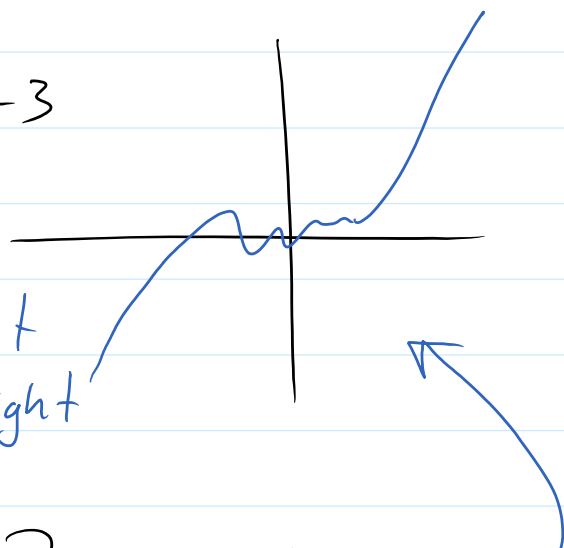
Ex: use the leading Coeff test to determine the end behavior of:

$$f(x) = x^3 + 3x^2 - x - 3$$

leading coeff: 1

degree: 3

The function falls on left
rises on right



$$f(x) = x^3 + 2x^2 - x + 3$$

$$f(x) = x(x-3)^4(x-1)^2 = x \cdot x^4 \cdot x^2 + \dots = x^7 + \dots$$

end behavior as

Ex: $f(x) = -4x^3(2x-1)^2(x+5) = -4x^3 \cdot (2x)^2 \cdot x + \dots$
 $= -4x^3 \cdot 4x^2 \cdot x + \dots$
 $= -16x^6 + \dots$

leading coeff: -16
degree: 6

Zeros of Polynomial Functions

Ex: Find all zeros of: $f(x) = (x^3 + 3x^2) - x - 3$
 $= x^2(x+3) - 1(x+3)$
 $= (x+3)(x^2-1)$
 $= (x+3)(x-1)(x+1)$

$$\begin{array}{c|c|c} x+3=0 & x-1=0 & x+1=0 \\ \hline \boxed{x=-3} & \boxed{x=1} & \boxed{x=-1} \end{array}$$

Ex: Find all zeros: $f(x) = -x^4 + 4x^3 - 4x^2 = 0$

$$x^2(-x^2 + 4x - 4) = 0$$

$$-x^2(x^2 - 4x + 4) = 0$$

$$-x^2(x-2)^2 = 0$$

$$x^2 = 0 \quad | \quad x - 2 = 0$$

$$\begin{array}{l|l} -x^2 = 0 & x-2 = 0 \\ \boxed{x=0} & \boxed{x=2} \end{array} \quad \begin{array}{l} -x^2(x-2) \neq 0 \\ \rightarrow -x \cdot x(x-2)(x-2) = 0 \end{array}$$

because 0 and 2 are zeros twice, we say that a zero of a polynomial has its multiplicity.

zero	multiplicity
0	2
2	2