MAC2311, Summer 2015

Final Exam

July 29, 2015

Name ______

- You will be told when to begin the work and when to terminate work on the examination. You must stop when instructed. Points may be deducted in case of violations.
- Please show your work to support your answers that require calculations. Correct but unsupported answers may not be given full credit.
- The use of a cell phone or other electronic communication devices during the examination is not allowed. The exam will be canceled and a grade of "0" will be assigned to anyone who opens a cell phone during the examination or if one is found on their seat or hand.

No graphing calculators are allowed

- 1. (10 points)
 - a) Find the average rate of change of $\frac{\tan(x)}{\tan(x)}$ over the interval $[0, \pi/3]$

b) Find the equation for a tangent line to $\frac{\tan(x)}{\tan(x)}$ at $x = \frac{\pi}{3}$

2. Find the limits

a) (5 points)
$$\lim_{x \to 0^-} \frac{e^x}{x\sqrt{x^2+4}}$$

b) (5 points)
$$\lim_{x \to 2} \frac{-1}{x-2}$$

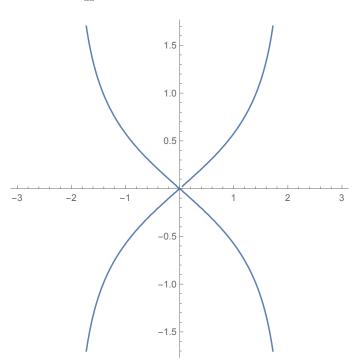
3. (10 points) Find the point (x, y), at which the graph of $y = \frac{\ln x}{x^2}$ has a horizontal tangent.

4. (10 points) Find the first and second derivatives.

a)
$$y = e^{x^3}$$

b) $y = \sec x$

5. (10 points) Graph of $x^2y^2 + x^2 = 4y^2$ is depicted below. Use implicit differentiation to find $y' = \frac{dy}{dx}$.



6. (10 points) Use logarithmic differentiation to find the derivative of y as a function of x.

$$y = x^x$$

7. (10 points) A rectangular fish tank is being filled at the constant rate of $40 \text{cm}^3/\text{sec.}$ The base of the tank has dimensions $20 \times 60 \text{cm.}$ What is the rate of change of the height of water in the tank?

8. (10 points) Find the intervals on which the function is increasing or decreasing.

$$y = \frac{2x}{x^2 + 4}$$

9. (10 points) Determine all critical points for the function. Determine which is local minimum or maximum.

$$y = 3x^2 - 96\sqrt{x}.$$

10. (10 points) A rectangular plot of farmland will be bounded on one side by a river and on the other three sides by a single-strand electric fence. With 2000m of wire at your disposal, what is the largest area you can enclose, and what are its dimensions?

11. (10 points) Evaluate the integral

$$\int_{\sqrt{2}}^{1} \frac{u^7}{2} - \frac{1}{u^3} \, du$$

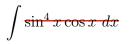
12. (10 points) Find the derivative

$$\frac{d}{dx} \int_{e^x}^6 \ln(x) \, dx$$

13. (10 points) Evaluate the integral $% \left(10\right) =0$

$$\int \frac{6x^2}{\sqrt{1+2x^3}} \ dx$$

14. (10 points) Evaluate the integral



15. (10 points) Find the area enclosed by y = x + 2 and $y = x^2$.