Homework 4

1. (40 points) Obtain the explicit forms of the generators of rotation in spin half space. Obtain also the egeinstates and eigenvalues of S^2 and S_z as well as S_x and S_y operators.

2. (40 points) For Pauli maticles prove the following relations: $[\sigma_{i}, \sigma_{j}] = 2 i \sum_{k} \epsilon_{ijk} \sigma_{k}$ $\sigma_{i} = \sigma_{i}^{\dagger} = \sigma_{i}^{-1}$ $\det \sigma_{i} = -1$ $(\hat{n} \cdot \hat{\sigma})^{2} = 1$ $\sigma_{i} \sigma_{j} + \sigma_{j} \sigma_{i} = 2 \delta_{ij}$ $(\sigma_{i})^{2} = 1$ $Tr \sigma_{i} = 0$ $\sigma_{i} \sigma_{j} = \delta_{ij} + i \sum_{k} \epsilon_{ijk} \sigma_{k}$

3. (30 points) Show that $e^{-i\frac{1}{2}n\cdot\sigma\theta} = I\cos(\theta/2) - in\cdot\sigma\sin(\theta/2)$ Calculate the rotational operators for the rotation around x, y and z axises.

4. (40 points) Present the brief description of Stern - Gerlach experiment.