Worksheet 1-20 - Graph Theory

1. (a) Sketch the complete bipartite graph $K_{3,4}$.
(b) What is the order and what is the size of $K_{p_{1}, p_{2}}$ ?
(c) When is $K_{p_{1}, p_{2}}$ a regular graph? Recall that a graph is called regular if all its vertices have the same degree.
(d) Describe the complement of $K_{3,4}, \overline{K_{3,4}}$, in terms of familiar graphs.
2. (a) Are the graphs $K_{3,3}$ and $C L_{3}$ isomorphic? Justify.
(b) Are the graphs $K_{3,3}$ and $M L_{3}$ isomorphic? Justify.
3. (a) Show that in any graph of order $p$, there is no open path of length larger than $p-1$.
(b) Show that in any graph of order $p$, there is no cycle of length larger than $p$.
(c) Do the statements in parts (a) and (b) remain true if "graph" is replaced by "general graph"?
4. (a) Sketch the graphs $\operatorname{circ}(7:\{1,2\})$ and $\operatorname{circ}(7:\{1,3\})$.
(b) Are the graphs in part (a) isomorphic? If yes, describe an isomorphism, if not, find a reason why they are not isomorphic.

Hint: It may be easier to consider the complements.

