

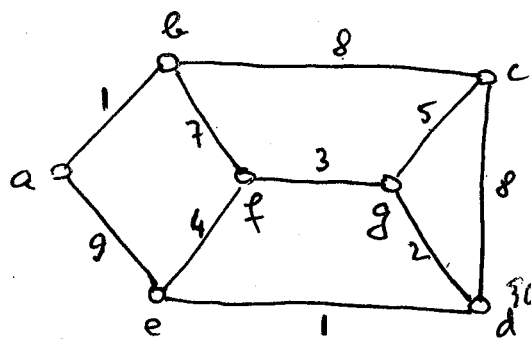
Worksheet 2-10 - Graph Theory

1. (a) Apply Kruskal's algorithm for the graph below to obtain a minim

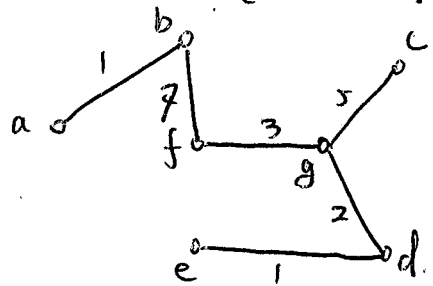
(b) For the same graph, apply now Prim's algorithm starting with the vert tree.

Note: The trees you get in parts (a) and (b) may not be the same, but their weights should be the same.

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(a) order edges: $e_1 = ab, e_2 = de, e_3 = dg, e_4 = gf, e_5 = fe, e_6 = gc, e_7 = bf, e_8 = cd, e_9 = cb, e_{10} = ac$



$W(T) = 1 + 7 + 3 + 5 + 2 + 1 = 19$

E(T)	Partition P	i	endpts of e
\emptyset	$\{a\}, \{b\}, \{c\}, \{d\}, \{e\}, \{f\}, \{g\}$	1	$\{a, b\}$
$\{ab\}$	$\{a, b\}, \{c\}, \{d\}, \{e\}, \{f\}, \{g\}$	2	$\{d, e\}$
$\{ab, de\}$	$\{a, b\}, \{c\}, \{d, e\}, \{f\}, \{g\}$	3	$\{d, g\}$
$\{ab, de, dg\}$	$\{a, b\}, \{c\}, \{d, e, g\}, \{f\}$	4	$\{g, f\}$
$\{ab, de, dg, gf\}$	$\{a, b\}, \{c\}, \{d, e, f, g\}$	5	$\{f, e\}$
no change	no change	6	$\{g, c\}$
$\{ab, de, dg, gf, gc\}$	$\{a, b\}, \{c, d, e, f, g\}$	7	$\{b, f\}$
$\{ab, de, dg, gf, gc, bf\}$	$\{a, b, c, d, e, f, g\} = V(G) \rightarrow \text{STOP}$		

So, the final E(T) is $\{ab, de, dg, gf, gc, bf\}$.

(b)

E(T)	V(T)	$d(x_0, V(T))$	x_0
\emptyset	$\{c\}$	a: ∞ , b: 8, c: 0, d: 8, e: ∞ , f: ∞ , g: 5	g
$\{cg\}$	$\{c, g\}$	a: ∞ , b: 8, c: -, d: 2, e: ∞ , f: 3, g: -	d
$\{cg, gd\}$	$\{c, d, g\}$	a: ∞ , b: 8, c: -, d: -, e: 1, f: 3, g: -	e
$\{cg, gd, de\}$	$\{c, d, e, g\}$	a: 9, b: 8, c: -, d: -, e: -, f: 3, g: -	f
$\{cg, gd, de, gf\}$	$\{c, d, e, f, g\}$	a: 9, b: 7, c: -, d: -, e: -, f: -, g: -	b
$\{cg, gd, de, gf, fb\}$	$\{b, c, d, e, f, g\}$	a: 1, b: -, c: -, d: -, e: -, f: -, g: -	a
$\{cg, gd, de, gf, fb, ba\}$	$\{a, b, c, d, e, f, g\} = V(G)$	- - - - - - - -	STOP

so, the final E(T) is $\{cg, gd, de, gf, fb, ba\}$