Name: $\qquad$

## Panther ID:

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Exam 1
Calculus II
Spring 2019
To receive credit you MUST SHOW ALL YOUR WORK. Answers which are not supported by work will not be considered.

1. $(8 \mathrm{pts})$ Find the average value of $f(x)=\sec ^{2} x$ on the interval $[0, \pi / 4]$.
2. ( 8 pts ) Find $\int_{-2}^{2} \sqrt{4-x^{2}} d x$
3. $(8 \mathrm{pts})$ Find $\frac{d}{d x} \int_{0}^{\sqrt{x}} \cos \left(t^{2}\right) d t$
4. $(8 \mathrm{pts})$ Find $\int_{-1}^{1} \frac{1}{1+x^{2}} d x$
5. (8 pts) Find $\int_{1}^{e} \frac{(\ln x)^{3}}{x} d x$
6. $(8 \mathrm{pts})$ Find $\int_{0}^{1} x \sqrt{1+3 x} d x$
7. (8 pts) Use summation notation and then find the exact value of the sum:
$1+3+5+7+\ldots+2017+2019$
It's OK to leave your answer as a product.
8. (10 pts) Find the area of the region enclosed by the parabola $y=x^{2}-x$ and the line $y=2 x$. Sketch and computation are required.
9. (10 pts) (a) (3 pts) Sketch a graph of $y=\ln x$ and on this graph shade an area corresponding to $\int_{1}^{9} \ln x d x$.
(b) (3 pts) On your graph from part (a) or on a new graph, next mark the area corresponding to $R_{4}^{\text {right }}$, the right-endpoint Riemann sum approximation with 4 equal subdivisions of $\int_{1}^{9} \ln x d x$.
(c) (1 pts) Is $R_{4}^{\text {right }}$ on over-estimate or an under-estimate of the integral?
(d) (3 pts) Write the concrete expression corresponding to $R_{4}^{\text {right }}$. You don't have to simplify, but your answer should be in a calculator ready form.
10. ( $8+4 \mathrm{pts}$ ) Set up an integral (or integrals) to represent the volume of the solid obtained by rotating the region bounded by $y=\sqrt{x}, y=0$ and $x=4$ around the line $x=5$. Be sure to indicate which method you are using, cross-section or cylindrical shells. Computation is not required, but a picture is.
Bonus: Up to 4 bonus points if you correctly solve this problem both ways.
11. ( 8 pts ) Set up an integral (or integrals) to represent the surface area generated by revolving the graph of $x y=1,1 \leq y \leq 2$, around the $y$-axis. (Again, just the set-up of the integral is required, not the computation).
12. (10 pts) Choose ONE. If you do both, only the larger score will be considered for this problem, but the second score may give some bonus towards a previous problem where your score is smaller.
(A) State and prove the part of FTC about $\frac{d}{d x}\left(\int_{a}^{x} \cdots\right)$. You may use without proof MVT for integrals.
(B) Use integrals to show that the volume of a cone is given by $V=\frac{1}{3} h \cdot A_{\text {base }}$, where $h$ denotes the height of the cone (the distance from the vertex to the base) and $A_{\text {base }}$ denotes the area of the base. For simplicity, it's OK to consider just the case of a right circular cone, although the formula is valid for any cone (and any pyramid for that matter).
