Compute the following partial derivatives:

$$(1) \ \frac{\partial}{\partial x}(x^2y + 3xy^2 + \sin(x))$$

$$(2) \ \frac{\partial}{\partial x} (\tan(x^2 y))$$

$$(3) \frac{\partial}{\partial y} \left( \cos(xy) \sin(xy^2) \right)$$

$$(4) \frac{\partial}{\partial x} \left( \frac{x^2 + xy^3}{y \sin(x)} \right)$$

(5) 
$$\frac{\partial^2}{\partial x \partial y} \left( \sec(x^2 y + xy^2) \right)$$