1. (5 pts; 2effort +3 correctness) In each case, prove or disprove. To disprove, it is enough to give a counterexample. (Note that while a Venn diagram helps, it is not a substitute to a proof or a concrete counterexample.)
(a) $A \backslash(B \backslash C)=(A \backslash B) \backslash C$, for all sets $A, B, C$.
(b) $(A \cap B) \times C=(A \times C) \cap(B \times C)$, for all sets $A, B, C$.
2. (5 pts; 2effort +3 correctness) Consider the set $A=\{a, b, c, d\}$. In each case, give an example of a relation $\mathcal{R}$ on $A$ satisfying the conditions. Just give the example, no further justification is needed.
(a) $\mathcal{R}$ is symmetric, anti-symmetric, but not reflexive.
(b) $\mathcal{R}$ is reflexive, transitive, but not symmetric and not anti-symmetric.
