

NAME:

MAC2312/Quiz-8

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READ ME FIRST: Show me all the magic very neatly on the page, for I do not read minds. Use correct notation when presenting your computations and arguments. Use complete sentences. Remember this: "=" denotes "equals", " $\Rightarrow$ " denotes "implies", and " $\Leftrightarrow$ " denotes "is equivalent to". Since the answer consists of all the magic transformations, do not "box" your final results. Eschew obfuscation.

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1. (4 pts.) Find the general term of the sequence, starting with  $n = 1$ , determine whether the sequence converges, and if so, find its limit.

$$\frac{1}{3}, -\frac{1}{9}, \frac{1}{27}, -\frac{1}{81}, \dots$$

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2. (2 pts.) Express the repeating decimal as a fraction.

$$0.4444\dots =$$

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3. (2 pts.) [Complete the following.] The harmonic series has the form

$$\sum_{k=1}^{\infty}$$

What is the sum of the harmonic series?

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4. (8 pts.) Determine whether the series converges, and if so, find its sum.

(a)  $\sum_{k=1}^{\infty} \left(-\frac{3}{4}\right)^{k-1}$

(b)  $\sum_{k=1}^{\infty} \frac{1}{(k+2)(k+3)}$

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5. (4 pts.) Find all values of  $x$  for which the series converges, and find the sum of the series for those values of  $x$ .

$$\frac{1}{x^2} + \frac{2}{x^3} + \frac{4}{x^4} + \frac{8}{x^5} + \frac{16}{x^6} + \dots$$