

**NAME:**

**MAC2312/Quiz-9**

---

READ ME FIRST: Show me all the magic very neatly on the page, for I do not read minds. Use correct notation when presenting your computations and arguments. Use complete sentences. Remember this: "=" denotes "equals", " $\Rightarrow$ " denotes "implies", and " $\Leftrightarrow$ " denotes "is equivalent to". Since the answer consists of all the magic transformations, do not "box" your final results. Eschew obfuscation.

---

1. (4 pts.) Use ratio test to determine whether the series converges, If the test is inconclusive, say so.

$$\sum_{k=1}^{\infty} \frac{3^k}{k!}$$

---

2. (4 pts.) Use root test to determine whether the series converges. If the test is inconclusive, say so.

$$\sum_{k=1}^{\infty} \left( \frac{3k+2}{2k-1} \right)^k$$

---

3. (4 pts.) Use comparison test to show the following series diverges.

$$\sum_{k=1}^{\infty} \frac{\ln(k)}{k}$$

---

4. (4 pts.) Apply the divergence test and state what it tells you about each of the following series.

(a)  $\sum_{k=1}^{\infty} \cos(k\pi)$

(b)  $\sum_{k=1}^{\infty} \frac{1}{\sqrt{k}}$

---

5. (4 pts.) Confirm that the integral test is applicable and then use it to determine whether the following series converges:

$$\sum_{k=1}^{\infty} \frac{1}{1+9k^2}$$