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**Read Me First:** Show all essential work neatly. Use correct notation when presenting your computations. Write using complete sentences. In particular, be very careful when using "=", **equals**, and " $\Rightarrow$ ", **implies**. Do not "box" your answers. Communicate.

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1. (5 pts.) If  $\theta = 135^\circ$ , what is the radian measure of  $\theta$  as an exact multiple of  $\pi$ ?  $\theta = 3\pi/4$

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2. (5 pts.) If  $\theta = 11\pi/6$  in radian measure, what is the value of  $\theta$  in degrees?  $\theta = 330^\circ$

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3. (5 pts.) If  $s = 8$  meters is the length of an arc of a circle of radius  $r = 6$  meters subtended by a central angle  $\theta$ , what is the exact value of  $\theta$  in degrees?  $\theta = (240/\pi)^\circ$

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4. (5 pts.) If  $\theta = 61^\circ 35' 20''$ , convert  $\theta$  to a decimal in degrees rounded to two decimal places.  $\theta = 61.59^\circ$

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5. (5 pts.) If  $\theta = 28.511^\circ$ , convert  $\theta$  to  $D^\circ M' S''$  form with the answer rounded to the nearest second.  $\theta = 28^\circ 30' 40''$

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6. (5 pts.) An object is traveling around a circle with a radius of 20 meters. Suppose that in 20 seconds a central angle of  $2/3$  radian is swept out. What is the angular speed  $\omega$  of the object, and what is the linear speed  $v$  of the object? Here give the exact value of the item followed by its decimal approximation.  
 $\omega = (1/30)$  radians/sec.  $\approx .033\bar{3}$  radians/sec.  
 $v = (2/3)$  meters/sec.  $\approx .66\bar{6}$  meters/sec.

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7. (5 pts.) If  $\theta$  is an acute angle, and  $\cos(\theta) = 2/3$ , obtain the exact values for the remaining ~~four~~ trigonometric functions.  
 $\tan(\theta) = 5^{1/2}/2$ ;  $\cot(\theta) = 2/5^{1/2}$ ;  $\sec(\theta) = 3/2$ ;  
 $\csc(\theta) = 3/5^{1/2}$ ;  $\sin(\theta) = 5^{1/2}/3$

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8. (5 pts.) If the point  $(-5, 4)$  is on the terminal side of an angle  $\theta$ , obtain the exact value of each of the six trigonometric functions of  $\theta$ .  
 $\sin(\theta) = 4/(41)^{1/2}$ ;  $\cos(\theta) = -5/(41)^{1/2}$ ;  
 $\tan(\theta) = -4/5$ ;  $\cot(\theta) = -5/4$ ;  $\sec(\theta) = -(41)^{1/2}/5$ ;  
 $\csc(\theta) = (41)^{1/2}/4$

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9. (5 pts.) What is the reference angle  $\theta_r$  for an angle  $\theta = -195^\circ$ ?  $\theta_r = 15^\circ$

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10. (5 pts.) Suppose  $\cos \theta = -(1/5)$  and  $\tan \theta > 0$ . What is the exact value of each of the remaining trigonometric functions?

$$\sec(\theta) = -5; \quad \tan(\theta) = (24)^{1/2}; \quad \sin(\theta) = -(24)^{1/2}/5;$$

$$\csc(\theta) = -5/(24)^{1/2}; \quad \cot(\theta) = 1/(24)^{1/2};$$

11. (18 pts.) Fill in the following table with the information requested concerning domain, range, and period.

Function Name	Domain (in radians)	Range	Period (in radians)
$\cot(\theta)$	B, below.	$\mathbb{R}$	$\pi$
$\sec(\theta)$	A, below.	$(-\infty, -1] \cup [1, \infty)$	$2\pi$
$\tan(\theta)$	A, below.	$\mathbb{R}$	$\pi$
$\sin(\theta)$	$\mathbb{R}$	$[-1, 1]$	$2\pi$
$\cos(\theta)$	$\mathbb{R}$	$[-1, 1]$	$2\pi$
$\csc(\theta)$	B, below.	$(-\infty, -1] \cup [1, \infty)$	$2\pi$

$$A = \{ x \in \mathbb{R} : x \neq (2k + 1)(\pi/2), k \text{ any integer} \}$$

$$B = \{ x \in \mathbb{R} : x \neq k\pi, k \text{ any integer} \}$$

12. (2 pts.) Use a calculator to obtain the approximate value of each of the following expressions. Round your answer to two decimal places.  $\sin 10 \approx -.54$   $\sin 10^\circ \approx .17$

13.,14.,15.: Partial graphs may be found in the text. They generally don't show two periods that are symmetric with respect to the origin.